



Sunyaev-Zel'dovich Effect

Karisa Zdanky
ASTR 8400



Moving Cluster

**Trigonometric
Parallax**



**What IS the
SZ Effect?**



The Namesake



Rashid Sunyaev

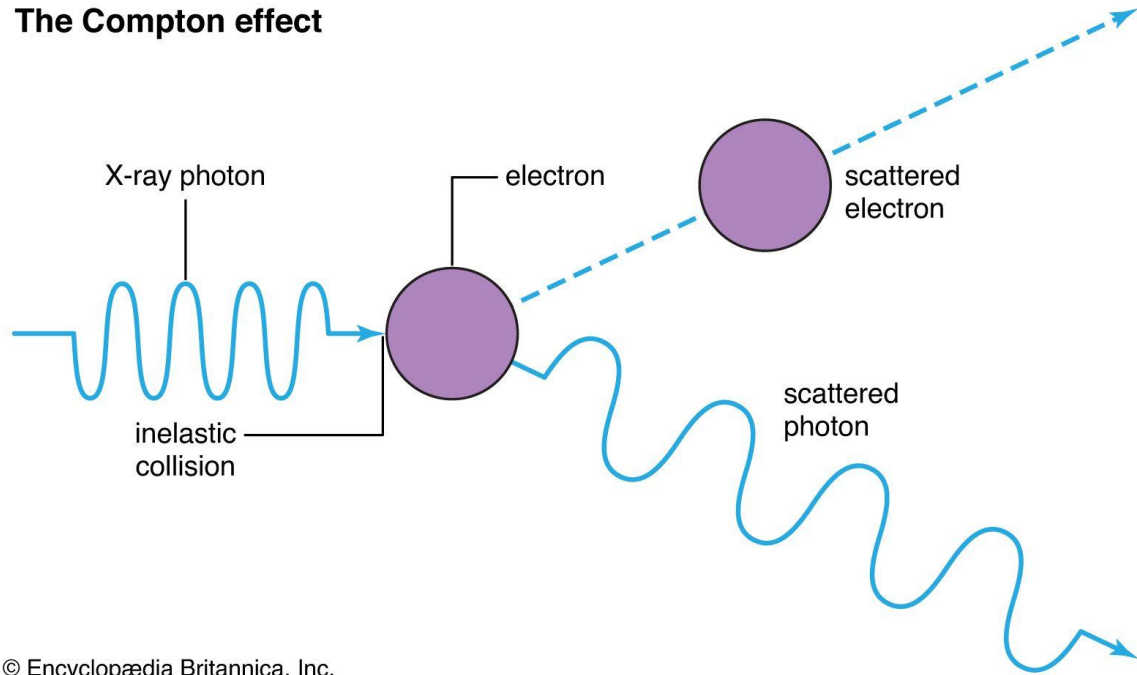


Yakov Zel'dovich

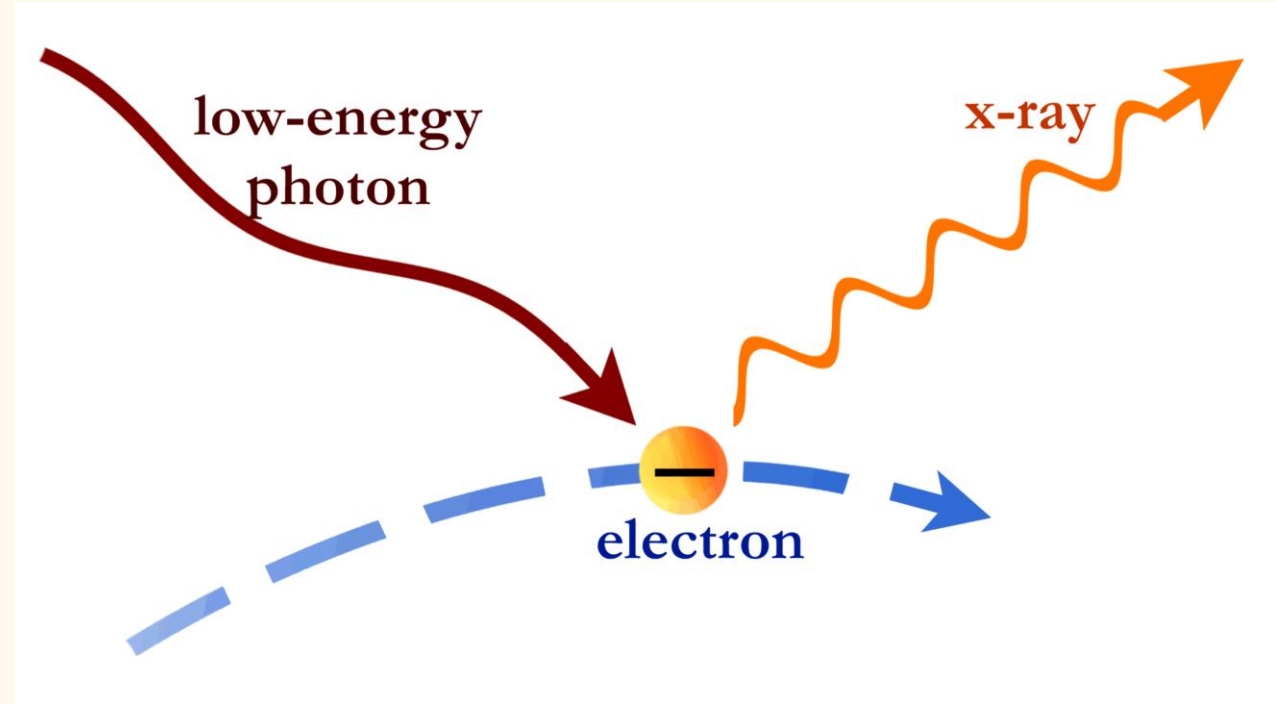


Compton Scattering

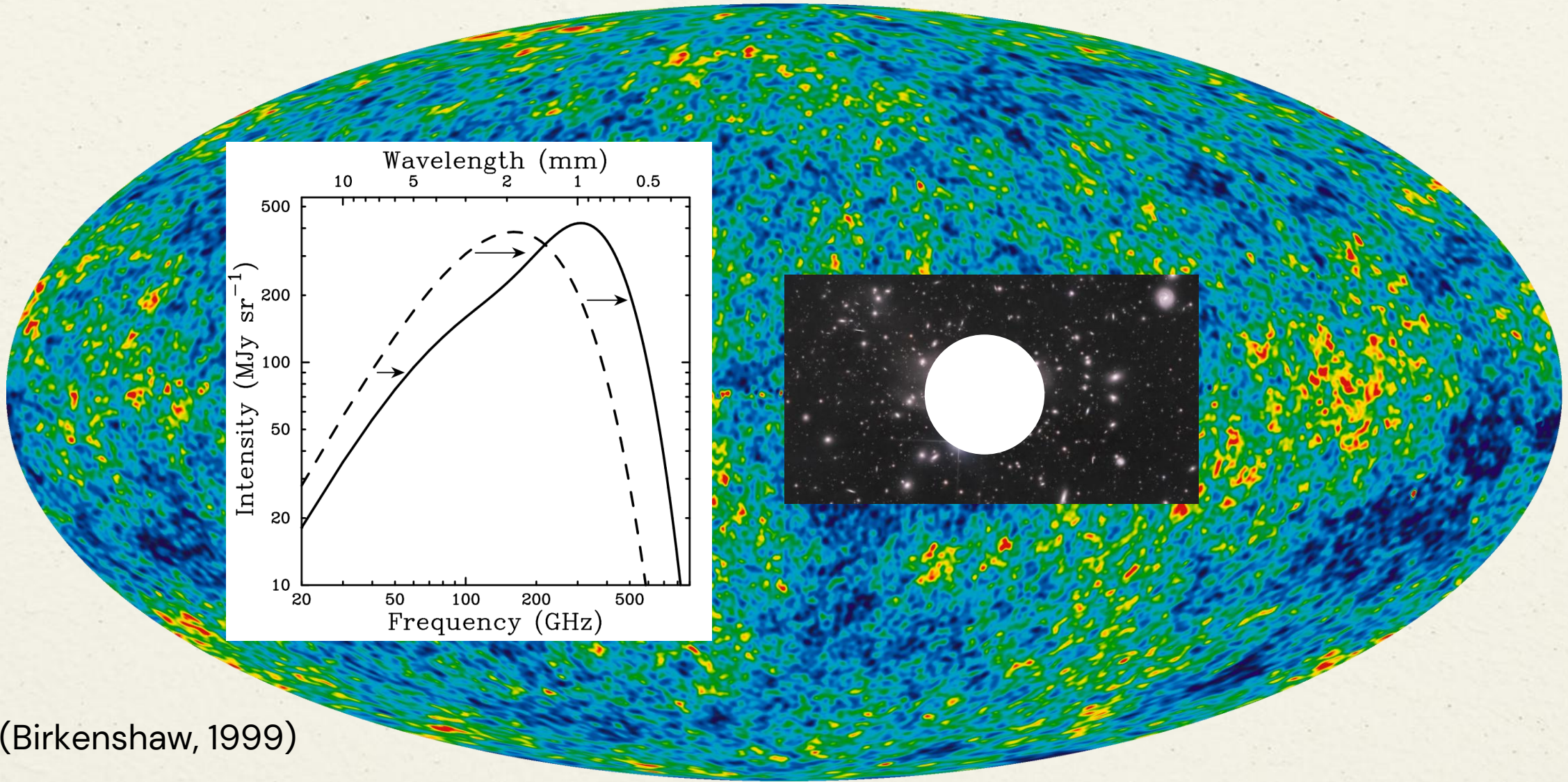
The Compton effect



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The SZ Effect in Action



(Birkinshaw, 1999)

(Sunyaev and Zel'dovich, 1970, 1972, 1980)



Observable!

RX J1347.5-1145

ALMA
(ESO/NAOJ/NRAO)/T.
Kitayama (Toho University,
Japan)/ESA/Hubble &
NASA

Two Main Types of SZ Effects

Thermal Effect

High energy in electrons is due to **temperature**

Kinetic Effect

High energy in electrons is due to **bulk motion**

Both play a part in finding the distance!

(Reese, 2004)
(Birkenshaw, 1999)

How do we find the distance?

$$\Delta T_{SZE} \sim \int d\ell n_e T_e$$

electron
temperature

SZE spectral
distortion of the
CMB

along the
line-of-sight

electron
density

angular-
diameter
distance!

$$d\ell = D_A d\zeta$$

**But wait!
There's
more...**

We need the X-Ray emission too!

$$S_x \sim \int d\ell n_e^2 \Lambda_{eH}$$

X-Ray
emission

electron
density

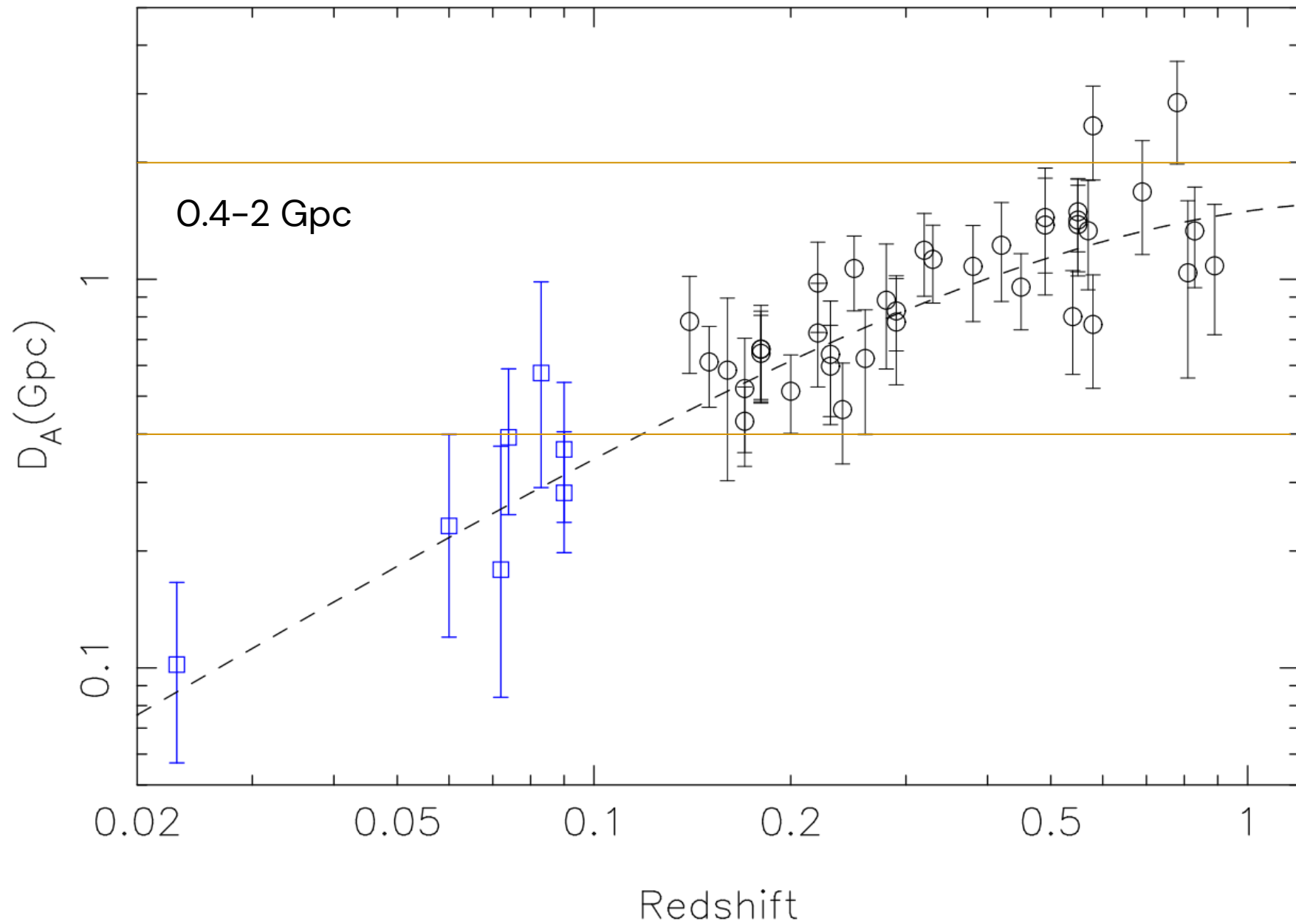
X-Ray cooling
function

Finding Distance

$$D_A \propto \frac{(\Delta T_0)^2 \Lambda_{eH0}}{S_{x0} T_{e0}^2} \frac{1}{\theta_c}$$

Characteristic scale
along line-of-sight
(depends on chosen
density model)

Evaluated along line-
of-sight through
center of cluster



(Bonamente, 2006)

Pros and Cons

Pros

- Distances are independent of the rest of the extragalactic distance ladder (no standard candles necessary!)
- Because independent of distance, can locate very distant clusters!
- Redshift independent (works for any redshift)
- Can make many other observations as well (mass, H_0 , etc.)

Cons

Cluster Asphericity

Most clusters aren't spherical in X-Ray/radio.
Assuming it is gives about 15% standard dev.

New data suggests that most galaxy clusters are elliptical! (Colaço, 2024)

Small Scale Clumps (Unlisted)

Can be left out of data (why it's unlisted).

However, clumpiness in intracluster medium smaller than Chanda res. can affect high-redshift clusters, giving a smaller distance.

Table 3. Sources of uncertainty in the measurement of D_A

Source	Effect on D_A	Reference
STATISTICAL CONTRIBUTIONS		
Galactic N_H	$\leq \pm 1\%$	(1)
Cluster asphericity	$\pm 15\%$	(2)
SZE point sources	$\pm 8\%$	(3)
Kinetic SZE effect	$\pm 8\%$	(4)
CMB anisotropy	$\leq 1\%$	(4)
X-ray background	$\pm 2\%$	(5)
SYSTEMATIC CONTRIBUTIONS		
Presence of radio halos	$+3\%$	(4)
X-ray absolute flux calibration (S_X)	$\pm 5\%$	(6)
X-ray temperature calibration (T_e)	$\pm 7.5\%$	(7)
SZE calibration	$\pm 8\%$	(4)

(1) This paper, Section 3.3.1.

(2) Sulkanen (1999).

(3) La Roche et al. (2006).

(4) Reese et al. (2002).

(5) This paper, Section 3.3.7.

(6) <http://asc.harvard.edu/cal/>.

(7) This paper, Section 3.3.8.

(Bonamente, 2006)

Cons

SZE Point Sources

Undetected radio point sources can create an underestimate of the cluster distance.

Kinetic SZE

Kinetic SZ effect comes into play. With typical assuming numbers, kinetic SZ effect is ~4% of thermal, creating 8% uncertainty.

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(Bonamente, 2006)

Cons

X-Ray Calibration

Typical X-ray calibration (from Chandra) gives about 7.5% uncertainty via calculations.

SZE Calibration

Typical SZE calibration gives about 8% uncertainty via calculations.

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(Bonamente, 2006)

Modern Use of the Sunyaev–Zel’dovich Effect

A Hubble Constant Estimate from Galaxy Cluster and type Ia SNe Observations

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²*Universidade Federal do Rio Grande do Norte, Departamento de Física Teórica e Experimental, 59300-000, Natal - RN, Brazil.*

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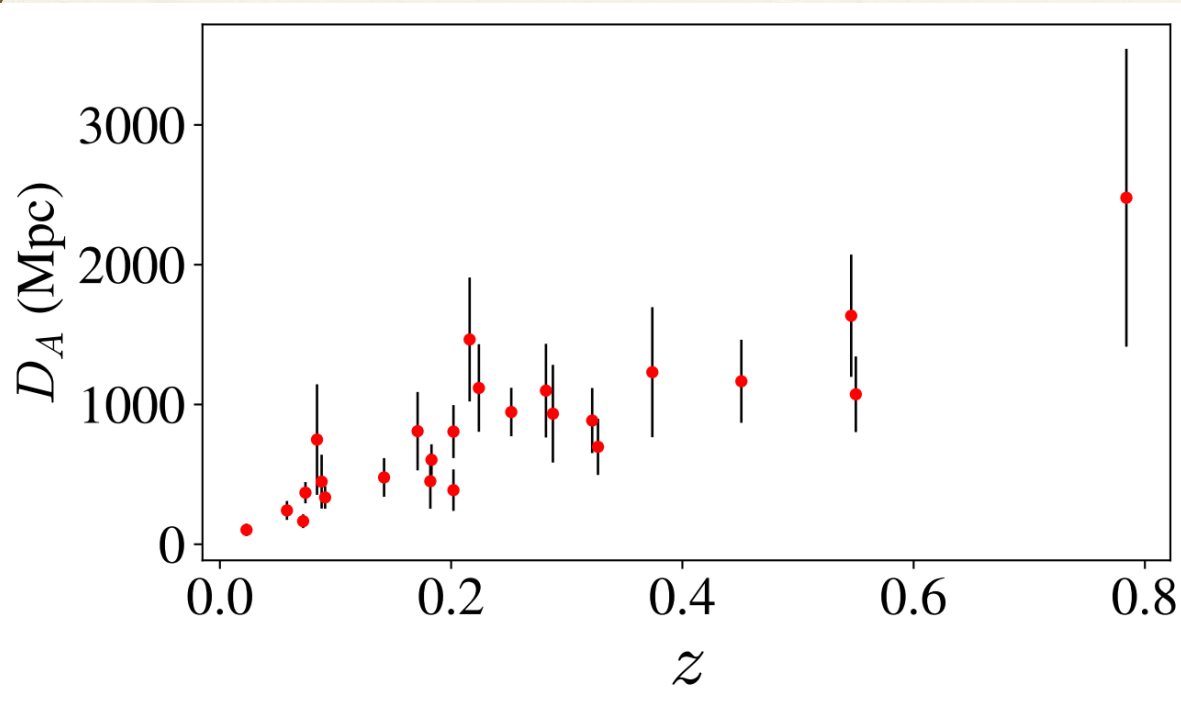
⁴*Instituto de Física, Universidade Federal do Rio Grande do Sul, 91501-970 Porto Alegre RS, Brazil*

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Avenida dos Astronautas 1758, São José dos Campos, 12227-010, SP, Brazil*

(2024!)

- “However, the usually assumed spherical geometry for galaxy clusters has been severely questioned... clusters exhibit preferably an elliptical surface brightness.”
- “Additionally, galaxy cluster angular diameter distance data... has also been rejected in several tests of the CDDR (cosmic distance duality relation).”
- “Moreover... it was predicted that dark matter halos show axis ratios typically of the order of ≈ 0.8 .”

Modern Use of the Sunyaev–Zel’dovich Effect



(Colaço et al, 2024)

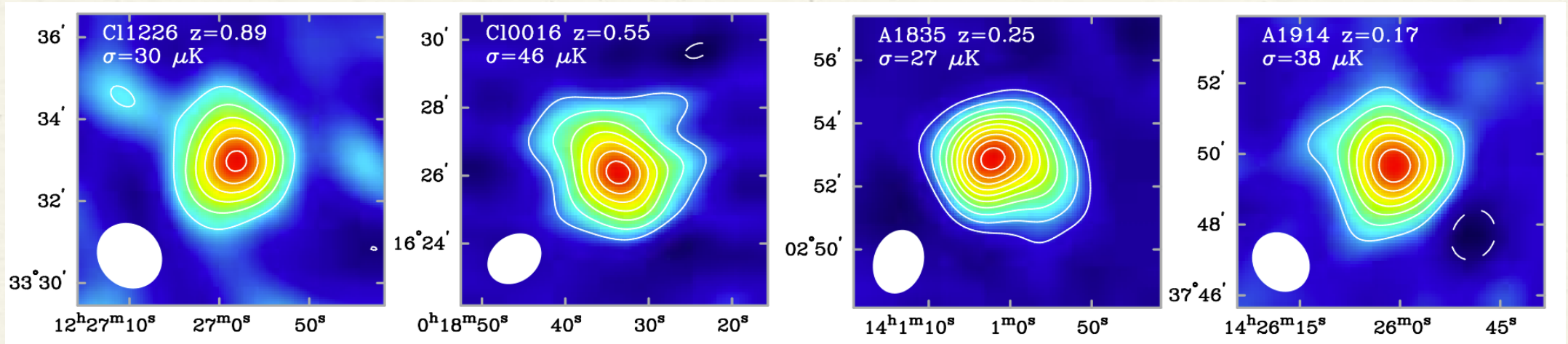
“...the galaxy cluster angular diameter determined from their SZE + X-ray observations provides an alternative method for determining direct cosmological distance. Our results further underscore the importance of actively pursuing observational efforts to obtain new galaxy cluster angular diameter distance samples through SZE and X-ray observations.”



ANGULAR DIAMETER DISTANCE			
Cluster	$D_c _{\text{cosm}}^a$ (Mpc)	$D_c _{\text{exp}}^{\text{circb}}$ (Mpc)	$D_c _{\text{exp}}^{\text{ell c}}$ (Mpc)
MS 1137.5+6625	1537 ⁺⁷¹ ₋₉₁	3179 ⁺¹¹⁰³ ₋₁₆₄₀	2479 ± 1023
MS 0451.6–0305	1322 ⁺⁵⁸ ₋₇₆	1278 ⁺²⁶⁵ ₋₂₉₉	1073 ± 238
Cl 0016+1609	1318 ⁺⁵⁸ ₋₇₆	2041 ⁺⁴⁸⁴ ₋₅₁₄	1635 ± 391
RX J1347.5–1145	1189 ⁺⁵² ₋₆₈	1221 ⁺³⁶⁸ ₋₃₄₃	1166 ± 262
A370.....	1063 ⁺⁴⁶ ₋₆₁	4352 ⁺¹³⁸⁸ ₋₁₂₄₅	1231 ± 441
MS 1358.4+6245	974 ⁺⁴¹ ₋₅₅	866 ⁺²⁴⁸ ₋₃₁₀	697 ± 183
A1995.....	964 ⁺⁴¹ ₋₅₄	1119 ⁺²⁴⁷ ₋₂₈₂	885 ± 207
A611.....	893 ⁺³⁸ ₋₅₀	995 ⁺³²⁵ ₋₂₉₃	934 ± 331
A697.....	880 ⁺³⁷ ₋₄₉	998 ⁺²⁹⁸ ₋₂₅₀	1099 ± 308
A1835.....	811 ⁺³⁷ ₋₄₅	1027 ⁺¹⁹⁴ ₋₁₉₈	946 ± 131
A2261.....	743 ⁺³¹ ₋₄₁	1049 ⁺³⁰⁶ ₋₂₇₂	1118 ± 283
A773.....	722 ⁺³⁰ ₋₄₀	1450 ⁺³⁶¹ ₋₃₃₂	1465 ± 407
A2163.....	686 ⁺²⁹ ₋₃₈	828 ⁺¹⁸¹ ₋₂₀₅	806 ± 163
A520.....	686 ⁺²⁹ ₋₃₈	723 ⁺²⁷⁰ ₋₂₃₆	387 ± 141
A1689.....	634 ⁺²⁷ ₋₃₅	688 ⁺¹⁷² ₋₁₆₃	604 ± 84
A665.....	632 ⁺²⁶ ₋₃₅	466 ⁺²¹⁷ ₋₁₇₉	451 ± 189
A2218.....	601 ⁺²⁵ ₋₃₃	1029 ⁺³³⁹ ₋₃₅₂	809 ± 263
A1413.....	515 ⁺²¹ ₋₂₉	573 ⁺¹⁷¹ ₋₁₅₁	478 ± 126
A2142.....	349 ⁺¹⁴ ₋₁₉	187 ⁺²¹² ₋₉₇	335 ± 70
A478.....	340 ⁺¹⁴ ₋₁₉	406 ⁺²³⁷ ₋₁₃₅	448 ± 185
A1651.....	327 ⁺¹⁴ ₋₁₈	373 ⁺²⁰² ₋₁₂₂	749 ± 385
A401.....	289 ⁺¹² ₋₁₆	610 ⁺⁵⁹³ ₋₂₅₄	369 ± 62
A399.....	282 ⁺¹² ₋₁₆	107 ⁺⁸⁵ ₋₄₁	165 ± 45
A2256.....	232 ⁺¹⁰ ₋₁₃	296 ⁺¹²⁷ ₋₉₀	242 ± 61
A1656.....	96 ⁺⁴ ₋₅	235 ⁺²¹⁸ ₋₉₈	103 ± 42

(Flippis, 2006)

(Reese, 2004)



Questions?